

November 28, 2007

Word Problems

- ① You have a rectangle of perimeter 440 cm and an area of 3025 cm^2 . What are its dimensions?



$$\begin{aligned}3025 &= l \cdot w \\2l + 2w &= 440 \\2l &= 440 - 2w \\l &= 220 - w\end{aligned}$$

sub $l = 220 - w$ into $3025 = l \cdot w$

$$\begin{aligned}3025 &= (220 - w)(w) \\3025 &= 220w - w^2 \\w^2 - 220w + 3025 &= 0\end{aligned}$$

$$w = \frac{220 \pm \sqrt{(-220)^2 - 4(1)(3025)}}{(2)1}$$

$$= \frac{220 \pm \sqrt{36300}}{2}$$

$$= \frac{220 \pm 110\sqrt{3}}{2}$$

$$w = 110 \pm 55\sqrt{3}$$

$$\begin{aligned}l &= 220 - w \\&= 220 - (110 \pm 55\sqrt{3}) \\&= 110 \pm 55\sqrt{3}\end{aligned}$$

② Find "m" to make the following a perfect square

$$y = x^2 + (m+1)x + 3m-5$$

$$\left(\frac{m+1}{2}\right)^2 = 3m-5$$

$$\frac{m^2+2m+1}{4} = 3m-5$$

$$m^2+2m+1 = 12m-20$$

$$m^2-10m+21 = 0$$

$$(m-3)(m-7) = 0$$

$$m=3, m=7$$

$$\begin{aligned} &x^2 + 10x + 25 \\ &(x+5)^2 \\ &(\text{half middle})^2 = \text{last} \end{aligned}$$

* Factorable when discriminant is a perfect square.

④ A rectangle has a length of 5cm more than the width. The area is 405 cm². Find length and width.

$$l = w + 5$$

$$405 = lw$$

$$405 = (w+5)(w)$$

$$405 = w^2 + 5w$$

$$w^2 + 5w - 405 = 0$$

$$w = \frac{-5 \pm \sqrt{5^2 - 4(1)(-405)}}{2(1)}$$

$$= \frac{-5 \pm \sqrt{1645}}{2}$$

$$l = \frac{-5 \pm \sqrt{1645}}{2} + \frac{10}{2}$$

$$= \frac{5 \pm \sqrt{1645}}{2}$$

⑤ The sum of a ⁺# + its square is 15. Find #

$$a^2 + a = 15$$

$$a^2 + a - 15 = 0$$

$$a = \frac{-1 \pm \sqrt{1 - 4(1)(-15)}}{2(1)}$$

$$= \frac{-1 \pm \sqrt{61}}{2}$$

$$= \frac{-1 + \sqrt{61}}{2}$$

⑥ Two consecutive even integers have squares that differ by 220. Find #s.

$$x+2$$

$$(x+2)^2 - (x)^2 = 220$$

$$x^2 + 4x + 4 - x^2 = 220$$

$$4x + 4 = 220$$

$$4x = 216$$

$$x = 54$$

$$54 + 56$$

